# Supplementary Information:A Bayesian Model to Analyze the Association of Rheumatoid Arthritis with Risk Factors and Their Interactions 

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## 1. SUPPLEMENTARY TABLES

## Proportion Male

|  | RA Prevalence | RA | No Arthritis | RA Female-Male Ratio |
| :---: | :---: | :---: | :---: | :---: |
| Literature reported | $\sim 0.5-1 \%$ | $\sim 25 \%$ | ~50\% | $\sim 2-3$ |
| NHANES (before preprocessing) | 3.01\% | 39.3\% | 49.6\% | 1.54 |
| NHANES (after preprocessing) | 6.55\% | 41.5\% | 52.7\% | 1.41 |

Table S1. RA prevalence, proportions of males in RA and no arthritis population, and female to male ratio in RA population are compared between literature reported values and NHANES data (before and after preprocessing).

| Study | Dataset | Risk Factors | RA Type | AUC |
| :--- | :---: | :---: | :---: | :---: |
| Karlson, et. al. [1] | NHS* | Age, sex, geographic region, smoking | Seropositive | 0.566 |
| Karlson, et. al. [1] | EIRA | Age, sex, geographic region, smoking | Seropositive | 0.626 |
| Karlson, et. al. [1] | NHS | Age, sex, smoking + 8 HLA, 14 SNP alleles | Seropositive | 0.660 |
| Karlson, et. al. [1] | EIRA | Age, sex, smoking + 8 HLA, 14 SNP alleles | Seropositive | 0.752 |
| Chibnik, et. al. [2] | NHS | GRS, age, smoking | Seronegative | 0.563 |
| Chibnik, et. al. [2] | NHS | GRS, age, smoking | Seropositive | 0.654 |
| Chibnik, et. al. [2] | NHS | GRS, age, smoking | Erosive and seropositive | 0.644 |
| Chibnik, et. al. [2] | NHS | GRS, age, smoking | Erosive | 0.712 |
| Karlson, et. al. [3] | NHS | Age, smoking, alcohol, education, parity | Seropositive | 0.655 |
| Karlson, et. al. [3] | EIRA | Age, smoking, alcohol, education, parity | Seropositive \& femalet | 0.632 |
| Karlson, et. al. [3] | EIRA | Age, smoking, alcohol, education | Seropositive \& male | 0.685 |
| This study | NHANES | Age, smoking | Self-reported | 0.748 |
| This study | NHANES | Age, sex, smoking | Self-reported | 0.772 |

Table S2. Comparison of predictive ability of current study against from previous works. Abbreviations: NHS, US Nurses' Health Studies I \& II; EIRA, Swedish Epidemiologic Investigation of RA; GRS, Genetic Risk Score. *All prediction using NHS was only performed on females. $\dagger$ "female" indicates prediction was only performed on female subjects; "male" indicates prediction was only performed on male subjects.

## 2. SUPPLEMENTARY FIGURE



Figure S1. Distributions of posterior variances of estimated regression coefficients from four Bayesian approaches used to predict RA with the training dataset; mean and variance of distributions are shown. (a) Regression model using only the 14 first-order variables. (b) Estimates for all 489 variables using regression coefficients derived from 52 synthetic variables after FAMD. (c) Estimates for all 489 variables using regression coefficients derived from 33 synthetic variables selected by GA. (d) regression model using all 489 variables without FAMD.


Figure S2. Marginal effects plots of (A) first-order variables age, BMI, and BP, (B) second-order interaction of age and BMI, and (C) third-order interaction of age, BMI, and BP, with first-order effects overlayed for comparison.

## REFERENCES

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