

SUPPORTING MATERIAL

Non-coding lincRNA-p21 and microRNA-155 Mediate the cellular adaptation to hypoxia

Here, we present the ordinary differential equations for the model and standard parameter values and the initial values of variables .

Appendix: Ordinary Differential Equations for the Model

$$\frac{d[\text{HIF-1}\alpha\text{m}]}{dt} = k_{\text{shifm}} - k_{\text{dhifm}}[\text{HIF-1}\alpha\text{m}] \quad (1)$$

$$k_{\text{dhifm}} = k_{\text{dhifm0}} + k_{\text{dhifm1}} \frac{[\text{miR-155}]}{[\text{miR-155}] + j_{55\text{hifmd}}} \quad (2)$$

$$\frac{d[\text{FIH-1}_{\text{ac}}]}{dt} = k_{\text{acfiH}} \frac{O_2}{O_2 + j_{O2\text{fiH}}} [\text{FIH-1}] - k_{\text{defiH}} [\text{FIH-1}_{\text{ac}}] \quad (3)$$

$$[\text{FIH-1}] = [\text{FIH-1}_{\text{tot}}] - [\text{FIH-1}_{\text{ac}}] \quad (4)$$

$$\begin{aligned} \frac{d[\text{HIF-1}\alpha]}{dt} = & k_{\text{thif}}[\text{HIF-1}\alpha\text{m}] - k_{\text{dhif}} \frac{j_{\text{dhif}}}{j_{\text{dhif}} + [\text{lincRNA-p21}]} [\text{HIF-1}\alpha] \\ & - k_{\text{dhiffiH}} \frac{j_{\text{dhiffiH}}}{j_{\text{dhiffiH}} + [\text{FIH-1}_{\text{ac}}]} [\text{HIF-1}\alpha] - k_{\text{aoh}} [\text{FIH-1}_{\text{ac}}] \frac{[\text{HIF-1}\alpha]}{[\text{HIF-1}\alpha] + j_{\text{hiffiH}}} \end{aligned} \quad (5)$$

$$\begin{aligned} \frac{d[\text{HIF-1}\alpha\text{-aOH}]}{dt} = & k_{\text{aoh}} [\text{FIH-1}_{\text{ac}}] \frac{[\text{HIF-1}\alpha]}{[\text{HIF-1}\alpha] + j_{\text{hiffiH}}} - k_{\text{poh}} [\text{PHD2}_{\text{ac}}] \frac{[\text{HIF-1}\alpha\text{-aOH}]}{[\text{HIF-1}\alpha\text{-aOH}] + j_{\text{hifphd}}} \\ & - k_{\text{dhif}} \frac{j_{\text{dhif}}}{j_{\text{dhif}} + [\text{lincRNA-p21}]} [\text{HIF-1}\alpha\text{-aOH}] \end{aligned} \quad (6)$$

$$\begin{aligned} \frac{d[\text{HIF-1}\alpha\text{-aOHpOH}]}{dt} = & k_{\text{poh}} [\text{PHD2}_{\text{ac}}] \frac{[\text{HIF-1}\alpha\text{-aOH}]}{[\text{HIF-1}\alpha\text{-aOH}] + j_{\text{hifphd}}} \\ & - k_{\text{dhifpoh}} \frac{j_{\text{dhifpoh}}}{j_{\text{dhifpoh}} + [\text{lincRNA-p21}]} [\text{HIF-1}\alpha\text{-aOHpOH}] \end{aligned} \quad (7)$$

$$\begin{aligned} \frac{d[\text{PHD2}_{\text{tot}}]}{dt} = & k_{\text{sphd0}} + k_{\text{sphd1}} \frac{[\text{HIF-1}\alpha]^n}{[\text{HIF-1}\alpha]^n + j_{\text{sphd1}}^n} + k_{\text{sphd1a}} \frac{[\text{HIF-1}\alpha\text{-aOH}]^n}{[\text{HIF-1}\alpha\text{-aOH}]^n + j_{\text{sphd1a}}^n} \\ & - k_{\text{dphd}} [\text{PHD2}_{\text{tot}}] \end{aligned} \quad (8)$$

$$\frac{d[\text{PHD2}_{\text{ac}}]}{dt} = k_{\text{acphd}} \frac{O_2}{O_2 + j_{\text{o2phd}}} [\text{PHD2}] - k_{\text{dephd}} [\text{PHD2}_{\text{ac}}] \quad (9)$$

$$[\text{PHD2}] = [\text{PHD2}_{\text{tot}}] - [\text{PHD2}_{\text{ac}}] \quad (10)$$

$$\begin{aligned} \frac{d[\text{miR-155}]}{dt} = & k_{\text{smiR1550}} + k_{\text{smiR1551}} \frac{[\text{HIF-1}\alpha]^n}{[\text{HIF-1}\alpha]^n + j_{\text{smiR1551}}^n} \\ & + k_{\text{smiR1551a}} \frac{[\text{HIF-1}\alpha\text{-aOH}]^n}{[\text{HIF-1}\alpha\text{-aOH}]^n + j_{\text{smiR1551a}}^n} - k_{\text{dmiR155}} [\text{miR-155}] \end{aligned} \quad (11)$$

$$\begin{aligned} \frac{d[\text{lincRNA-p21}]}{dt} = & k_{\text{sLAp210}} + k_{\text{sLAp21}} \frac{[\text{HIF-1}\alpha]^n}{[\text{HIF-1}\alpha]^n + j_{\text{sLAp21}}^n} \\ & + k_{\text{sLAp21a}} \frac{[\text{HIF-1}\alpha\text{-aOH}]^n}{[\text{HIF-1}\alpha\text{-aOH}]^n + j_{\text{sLAp21a}}^n} - k_{\text{dLAp21}} [\text{lincRNA-p21}] \end{aligned} \quad (12)$$

Table S1: Variables and their initial values

Variable	initial values	Variable	initial values	Variable	initial values
[HIF-1 α m]	1.5	[HIF-1 α -aOH]	1.04	[PHD2 _{ac}]	2.3
[FIH-1 _{ac}]	6.92	[HIF-1 α -aOHpOH]	0.14	[miR-155]	0.2
[HIF-1 α]	0.56	[PHD2 _{tot}]	5	[lincRNA-p21]	0.1

Table S2: Standard Parameter Values

Parameter	Description	Value	Reference
k_{shifm}	Induction rate of <i>HIF-1α</i> mRNA	0.0053	estimated
k_{dhifm0}	Basal degradation rate of <i>HIF-1α</i> mRNA	0.003	[1]
k_{dhifm1}	miR-155-dependent degradation rate of <i>HIF-1α</i> mRNA	0.006	estimated
j_{5shifmd}	Michaelis constant of miR-155-dependent <i>HIF-1α</i> mRNA degradation	2	estimated
[FIH-1 _{tot}]	Total concentration of FIH-1	10	estimated
k_{acfiH}	O_2 -dependent activation rate of FIH-1	3	estimated
j_{o2fiH}	Michaelis constant of O_2 -dependent FIH-1 activation	7	[2,3]
k_{defiH}	Deactivation rate of FIH-1	1	estimated
k_{thif}	Translation rate of <i>HIF-1α</i> mRNA	0.04	estimated
k_{dhif}	Primary degradation rate of HIF-1 α or HIF-1 α -aOH	0.02	[4]
j_{dhif}	Michaelis constant of repressing HIF-1 α or HIF-1 α -aOH degradation by lincRNA-p21	0.3	estimated
k_{poh}	PHD2-induced hydroxylation rate of HIF-1 α -aOH at proline residue	0.06	estimated
j_{hifphd}	Michaelis constant for HIF-1 α -aOH as a substrate of PHD2	3	estimated
k_{aoh}	FIH-1-induced hydroxylation rate of HIF-1 α at asparagine residue	0.06	estimated
j_{hiffiH}	Michaelis constant for HIF-1 α as a substrate of FIH-1	4	estimated
k_{dhiffiH}	FIH-1-related degradation rate of HIF-1 α	0.0032	estimated
j_{dhiffiH}	Michaelis constant of FIH-1-related HIF-1 α degradation	0.1	estimated

$k_{dhifpoh}$	Primary degradation rate of HIF-1 α -aOHpOH	0.34	[4]
$j_{dhifpoh}$	Michaelis constant of repressing HIF-1 α -aOHpOH degradation by lincRNA-p21	0.3	estimated
n	Hill coefficient of transactivating PHD2, miR-155 and lincRNA-p21 by HIF-1 α or HIF-1 α -aOH	4	estimated
k_{sphd0}	Basal induction rate of PHD2	0.03	estimated
k_{sphd1}	HIF-1 α -inducible production rate of PHD2	0.03	estimated
j_{sphd1}	Michaelis constant of HIF-1 α -dependent PHD2 production	6	estimated
k_{sphd1a}	HIF-1 α -aOH-inducible production rate of PHD2	0.02	estimated
j_{sphd1a}	Michaelis constant of HIF-1 α -aOH-dependent PHD2 production	10	estimated
k_{dphd}	Degradation rate of PHD2	0.006	estimated
k_{acphd}	O_2 -dependent activation rate of PHD2	1.8	estimated
j_{o2phd}	Michaelis constant of O_2 -dependent PHD2 activation	23	[2,3]
k_{dephd}	Deactivation rate of PHD2	1	estimated
$k_{smiR1550}$	Basal induction rate of miR-155	6.4E-5	estimated
$k_{smiR1551}$	HIF-1 α -inducible production rate of miR-155	0.0024	estimated
$j_{smiR1551}$	Michaelis constant of HIF-1 α -dependent miR-155 production	6.5	estimated
$k_{smiR1551a}$	HIF-1 α -aOH-inducible production rate of miR-155	0.0012	estimated
$j_{smiR1551a}$	Michaelis constant of HIF-1 α -aOH-dependent miR-155 production	6.5	estimated
$k_{dmiR155}$	Degradation rate of miR-155	0.00032	[5]
$k_{sLAp210}$	Basal induction rate of lincRNA-p21	0.002	estimated
k_{sLAp21}	HIF-1 α -inducible production rate of lincRNA-p21	0.08	estimated
j_{sLAp21}	Michaelis constant of HIF-1 α -dependent lincRNA-p21 production	5.7	estimated
$k_{sLAp21a}$	HIF-1 α -aOH-inducible production rate of lincRNA-p21	0.05	estimated
$j_{sLAp21a}$	Michaelis constant of HIF-1 α -aOH-dependent lincRNA-p21 production	5.8	estimated
k_{dLAp21}	Degradation rate of lincRNA-p21	0.02	estimated

Note: it is the relative rather than absolute value of O_2 level that makes sense, so for convenience, the oxygen level at normoxia is denoted as 21 and j_{o2phd} and j_{o2fih} are determined according to the relation between the K_m of PHD2 and FIH-1 activation for O_2 [2,3].

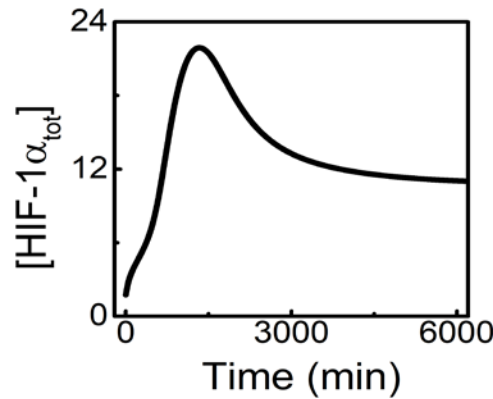


Figure S1: Time courses of $[HIF-1\alpha_{tot}]$ for 0.3% O_2

References

- [1] Bett, J. S., Ibrahim, A. F., et al. 2013. The P-body component USP52/PAN2 is a novel regulator of HIF1A mRNA stability. *Biochem J* 451(2): 185-194
- [2] Koivunen, P., Hirsia, M., et al. 2004. Catalytic properties of the asparaginyl hydroxylase (FIH) in the oxygen sensing pathway are distinct from those of its prolyl 4-hydroxylases. *J Biol Chem* 279(11): 9899-9904.
- [3] Qutub, A. A. and A. S. Popel (2006). "A computational model of intracellular oxygen sensing by hypoxia-inducible factor HIF1 alpha." *J Cell Sci* 119(Pt 16): 3467-3480.
- [4] Huang, L. E., Gu, J., Schau, M. and Bunn, H. F. 1998. Regulation of hypoxia inducible factor 1 α is mediated by an O₂-dependent degradation domain via the ubiquitin-proteasome pathway. *Proc. Natl. Acad. Sci. USA* 95, 7987-7992.
- [5] Gantier, M. P. 2010. New Perspectives in MicroRNA Regulation of Innate Immunity. *Journal of Interferon & Cytokine Research* 30: 283-289