

Supplementary Material

Carbon Dioxide Capture from Internal Combustion Engine Exhaust using Temperature Swing Adsorption

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Table A: Materials with lowest parasitic energies (PE) for CO₂ capture from coal flue gas [1]

Materials	PE, KJ/kg-CO ₂
Mg-MOF-74	727
PPN-6-CH2TETA	742
mmen-CuBTTri	752
NaX	754
MgX	760
NaA	765
CaA	784
CaX	785
MgA	793
SIFSIX-3-Zn	805
ZIF-36-FRL	829
PPN-6-CH2TAEA	835
PPN-6-SO3Li	846
Zn-MOF-74	850

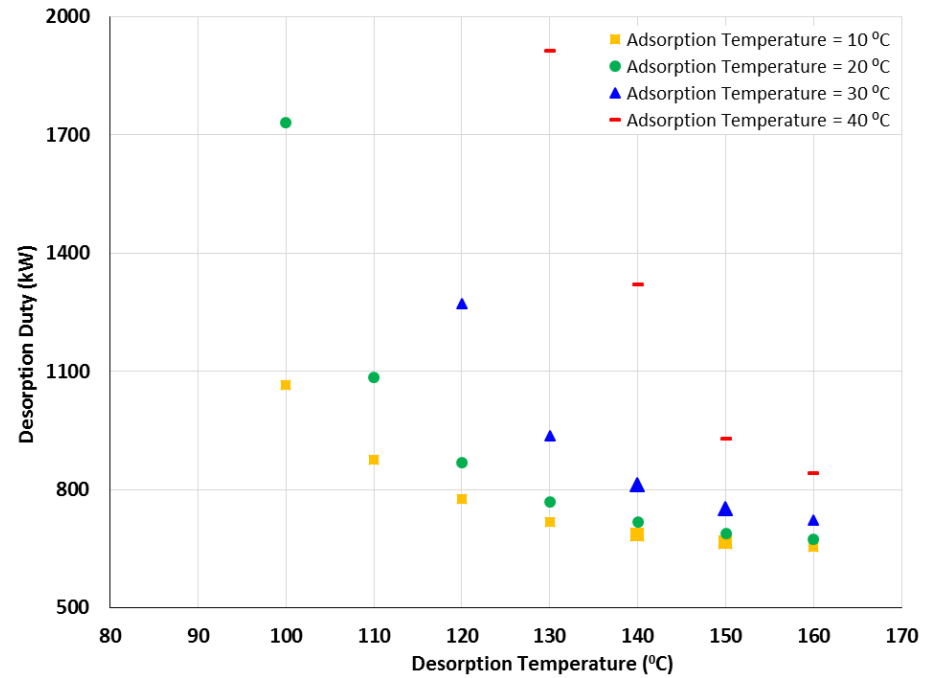


Figure A: Adsorption and desorption temperatures selection for PPN-6-CH2TETA [$T_{ad} = 30$ °C & $T_{des} = 150$ °C]

Table B: TSA model equations [2]

Component mass balance	$\varepsilon_t \frac{\partial c_i}{\partial t} + \frac{\partial(uc_i)}{\partial z} + \rho_b \frac{\partial q_i}{\partial t} = 0$	c = fluid phase conc. (mol/m ³) u = superficial gas velocity (m/s) q = solid phase conc. (mol/kg)
Overall mass balance	$\varepsilon_t \frac{\partial c}{\partial t} + \frac{\partial(uc)}{\partial z} + \rho_b \sum_{j=1}^N \frac{\partial q_j}{\partial t} = 0$	q^* = solid phase equilibrium conc. (mol/kg) q^s = solid phase saturation conc. (mol/kg) t = time (s)
Mass transfer	$\frac{\partial q_i}{\partial t} = k_i(q_i^* - q_i)$	z = vertical/height coordinate (m) k = overall mass transfer coefficient (1/s)
Energy balance	$\begin{aligned} &(\varepsilon_t C_g + \rho_b C_s + \rho_b C_{ads}) \frac{\partial T}{\partial t} + u C_g \rho \frac{\partial T}{\partial z} \\ &- \rho_b \sum_{j=1}^N (-\Delta H_j) \frac{\partial q_j}{\partial t} + \frac{h_L}{D} (T - T_{media}) = 0 \end{aligned}$	C_g = heat capacity of gas (J/[K.m ³]) C_s = heat capacity of solid (J/[K.kg]) C_{ads} = adsorbed phase heat capacity (J/[K.kg]) ΔH = heat of adsorption (J/mol) h_L = heat transfer coefficient (J/m ² .s.K)
Momentum balance (Ergun equation)	$\frac{\partial p}{\partial z} = - \frac{150\mu(1 - \varepsilon_b)^2}{\varepsilon_b^3 d_p^2} u - \frac{1.75(1 - \varepsilon_b)\rho}{\varepsilon_b^3 d_p} u u$	D = column inner diameter (m) p = fluid pressure (Pa)
q equilibrium & K calculations	$\begin{aligned} &q_i^*(q_i^s + K_i C_i RT) - q_i^s K_i C_i RT = 0 \\ &K_i - K_i^{ref} e^{\left[\frac{H_i^{ads}}{R \left(\frac{1}{T} - \frac{1}{T_{ref}} \right)} \right]} = 0 \end{aligned}$	d_p = particle diameter (m) K = Henry coefficient (mol/[kg.Pa]) R = ideal gas constant (J/K.mol) T = temperature (K)
Bed area & feed flow rate	$\begin{aligned} &A = \frac{\pi D^2}{4} \\ &Q_{v,f} = \frac{\dot{m}_f}{\rho} \end{aligned}$	T_{amb} = ambient temperature (K) H_{ads} = heat of adsorption (J/mol) A = area (m ²)
Auxiliary relationships	$\begin{aligned} &\sum_{j=1}^N y_j = 1 \\ &c_i = y_i * \frac{p}{RT} \\ &p - \sum_{j=1}^N C_j RT = 0 \end{aligned}$	$Q_{v,f}$ = volumetric feed flow rate (m ³ /s) $\dot{m}_f$ = feed mass flow rate (kg/s) y = component mass fraction L = bed height (m) μ = dynamic viscosity (kg/[m.s]) ρ = fluid phase density (kg/m ³)

	$c_{tot} = \sum_{j=1}^N C_j$	ρ_b = bed density (kg/m ³) ε_t = overall void fraction ε_b = bed void fraction i = component number N = total number of components ref = reference, tot = total
Initial and boundary conditions for adsorption	$y_{CO_2} _{z=0} = y_{CO_2,feed}$ $T _{z=0} = T_{feed}$ $y_{CO_2} _{z=L} = y_{CO_2,residue}$ $\frac{\partial T}{\partial z} _{z=1} = 0, \frac{\partial c}{\partial z} _{z=1} = 0, \frac{\partial P}{\partial z} _{z=1} = 0$	
Parameters values	$D = 0.25$ m, $d_p = 0.003$ m, $h_L = 3000$ (J/m ² .s.K), $k = 0.3$ (1/s) $L = 1$ (m), $T_{feed} = 303$ (K), $T_{amb} = 293$ (K), $\varepsilon_b = 0.4$, $\varepsilon_t = 0.742$	

Table C: PPN-6-CH2TETA parameters values [1].

Material's Parameter	Value
Heat of adsorption for CO ₂ (kJ/mol), H_{ads}	-48.23
Heat of adsorption for N ₂ (kJ/mol), H_{ads}	-18.29
Henry coefficient for CO ₂ (mol/kg.Pa), K_{ref}	0.00652
Henry coefficient for N ₂ (mol/kg.Pa), K_{ref}	6.99e-07
Saturation loading for CO ₂ (mol/kg), q^s	4.77
Saturation loading for N ₂ (mol/kg), q^s	0.04
Density (kg/m ³), ρ_b	883.8
Heat capacity (J/kg.K), C_s	985

- In this study, N₂ and O₂ co-adsorption has not been considered. For the modeling/simulation purpose, O₂ is considered as N₂.
- The adsorbent material was assumed to be fully regenerated prior to every adsorption step. This assumption is reasonable for Case 1 (desorption in parking lot). For Cases 2 & 3, the adsorbent material cannot be fully regenerated, and a small fraction of CO₂ will remain in the adsorbent material before the start of a new TSA cycle.
- The adsorption model has been solved, until 90% CO₂ presents in the fresh feed is captured by the material. The CO₂ capture rate decreases with increase in the adsorption time.
- Percentage CO₂ capture rate is calculated, as: (total inlet CO₂ – total outlet CO₂)/total inlet CO₂×100. Total inlet CO₂ and total outlet CO₂ are calculated by integrating/summing inlet CO₂ to the bed and outlet CO₂ from the bed, for entire adsorption time.
- For a specific feed flow rate and composition, heat of adsorption is calculated using total heat removed and amount of CO₂ attached to the material.
- In this study, detailed heat exchange inside the adsorption bed has not been studied.

Exergy Calculations for 1 liter Diesel [3, 4]

1. Diesel fuel:

$$\varepsilon_{1,f} = 1.0338 \times \text{LHV} = 38.53 \text{ MJ}$$

[LHV = 37.27 for 1 liter diesel]

2. Mechanical power:

$$\varepsilon_{1,mp} = 13.05 \text{ MJ}$$

3. Engine cooling:

$$\varepsilon_{1,ec} = Q \times (1 - T_0/T) = 10.02 \times (1 - 298/393) = 2.42 \text{ MJ}$$

[T = 393 K]

4. Engine exhaust:

$$\varepsilon_{1,ee} = Q \times (1 - T_0/T) = 8.24 \times (1 - 298/524.4) = 3.56 \text{ MJ}$$

[T = 524.4 K: log mean of 773 and 338.3 K]

$$\varepsilon_{2,ee} = Q \times (1 - T_0/T) = 5.97 \times (1 - 298/316.8) = 0.35 \text{ MJ}$$

[T = 316.8 K: log mean of 338.3 and 298 K]

5. Cooling and adsorption:

$$\varepsilon_{1,ca} = Q \times (1 - T_0/T) = 3.96 \times (1 - 298/358.6) = 0.67 \text{ MJ}$$

[T = 358.6 K: log mean of 423 and 303 K]

$$\varepsilon_{2,ca} = Q \times (1 - T_0/T) = 4.21 \times (1 - 298/303) = 0.07 \text{ MJ}$$

[T = 303 K]

6. Heating and desorption:

$$\varepsilon_{1,hd} = - Q \times (1 - T_0/T) = - 3.74 \times (1 - 298/358.6) = - 0.63 \text{ MJ}$$

[T = 358.6 K: log mean of 303 and 423 K]

$$\varepsilon_{2,hd} = - Q \times (1 - T_0/T) = - 4.21 \times (1 - 298/423) = - 1.24 \text{ MJ}$$

[T = 423 K]

7. Inter-stage CO₂ cooling:

$$\varepsilon_{1,is} = Q \times (1 - T_0/T) = 0.22 \times (1 - 298/358.6) = 0.04 \text{ MJ}$$

[T = 358.6 K: log mean of 423 and 303 K]

$$\varepsilon_{2,is} = Q \times (1 - T_0/T) = 0.45 \times (1 - 298/403.6) = 0.12 \text{ MJ}$$

[T = 403.6 K: log mean of 527.4 and 303 K]

$$\varepsilon_{3,is} = Q \times (1 - T_0/T) = 0.42 \times (1 - 298/401.1) = 0.11 \text{ MJ}$$

[T = 401.1 K: log mean of 518.4 and 305 K]

$$\varepsilon_{4,is} = Q \times (1 - T_0/T) = 0.52 \times (1 - 298/300.6) = 0.004 \text{ MJ}$$

[T = 300.6 K: log mean of 305 and 298 K]

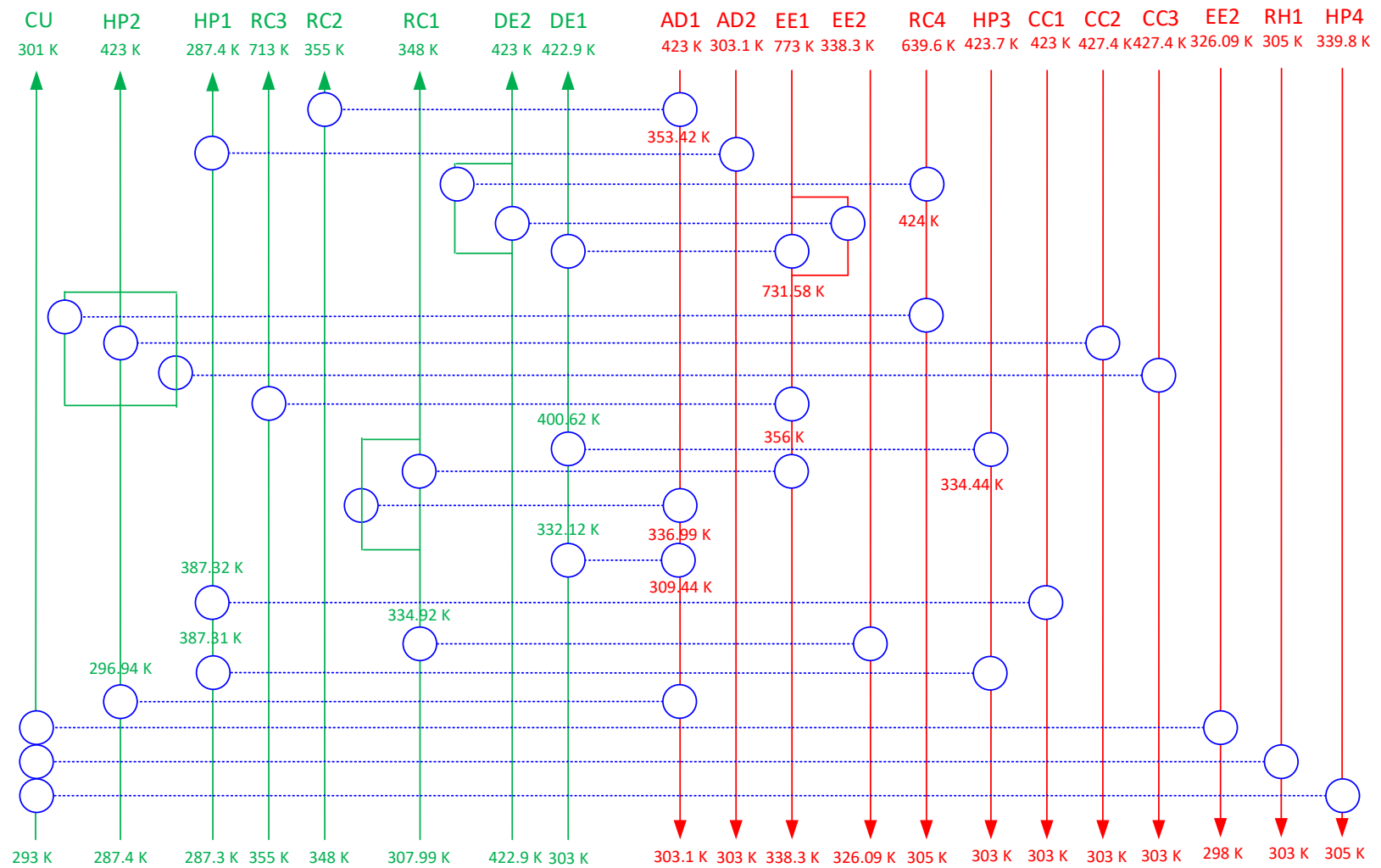


Figure B: Grid representation of heat exchanger network

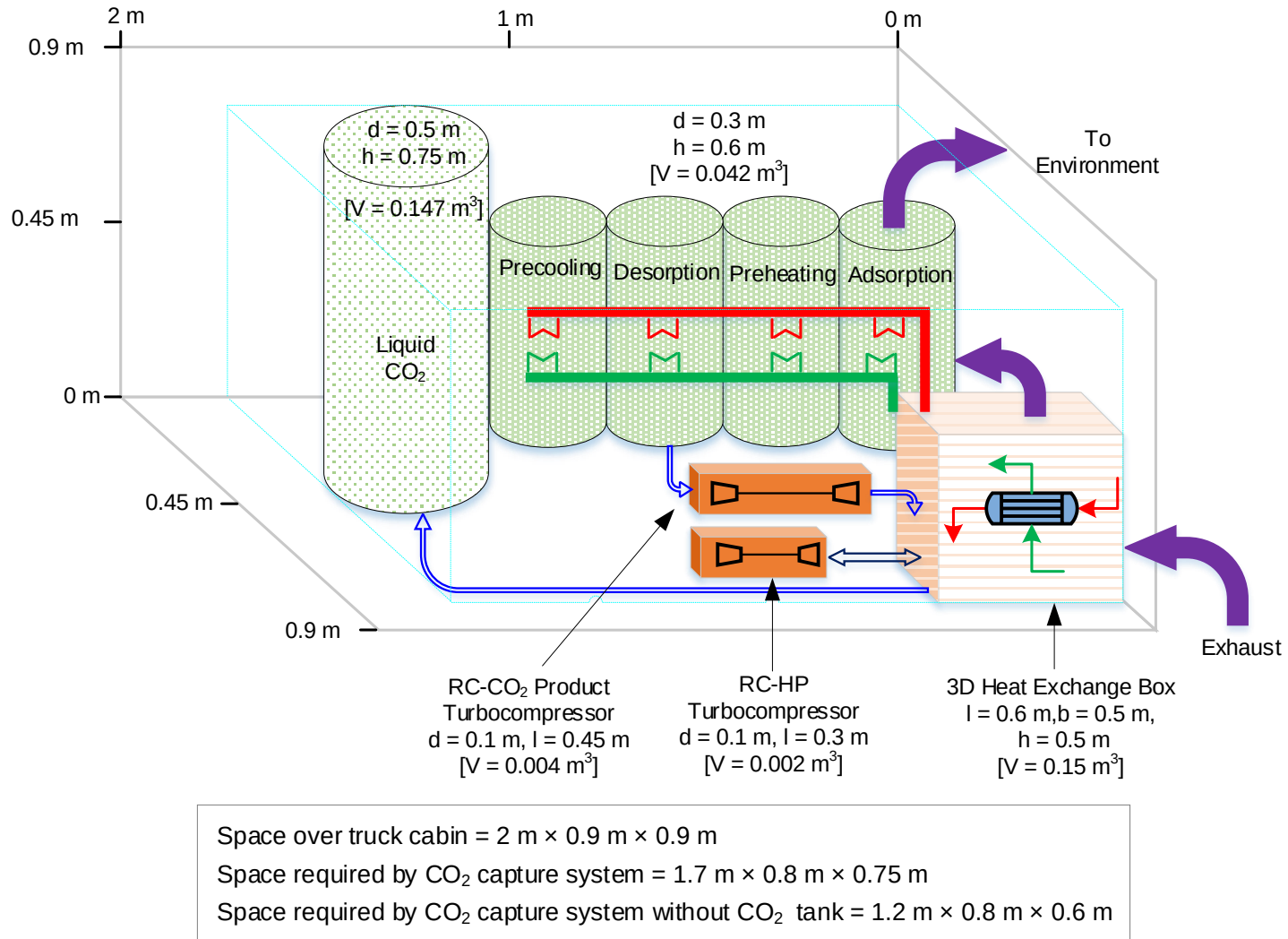


Figure C: Estimated volume of the CO₂ capture and storage system for delivery truck (size of turbocompressor is estimated based on Casey et al. [5]; Volume of 3D heat exchange box is estimated with 100 m²/m³ surface area to volume ratio)

Table D: Conversion of 1 kg of CO₂ into green fuels [6]

	Methane	Methanol	DME	Gasoline
Fuel, kg	0.37	0.67	0.46	0.26
Electricity consumptions, MJ	24.5	20.5	21.3	18.8
Photovoltaic panels area (Switzerland), m ²	7.1	5.9	6.2	5.4

Table E: Weight, payload and diesel consumption for different vehicles

	Weight (kg)	Payload (kg)	Diesel Used per 100 km, l	Diesel Used & CO ₂ produced in 250 km Travel				References
				Diesel Used, l	Product CO ₂ , kg	Product CO ₂ , l	Storage Tank, kg	
Car	1678	454	6.5	16.25	34.29	48.09	34.62	7, 8, 16
SUV	1746	680	11	27.5	58.03	81.38	58.59	7, 8, 16
Pickup Truck	2563	1678	13	32.5	68.58	96.18	69.25	7, 8, 16
Van/Minibus	3708	2381	11	27.5	58.03	81.38	58.59	7, 8, 16
School Bus	5897	5216	22	55	116.05	162.76	117.19	7, 8, 16
City Bus	5897	8391	58	145	305.95	429.09	308.95	7, 8, 16
City Hybrid Bus	5897	8391	45	112.5	237.38	332.92	239.70	7, 8, 16
City Delivery	4423	3946	21.2	53	111.83	156.84	112.93	7, 9, 16
Regional Delivery Truck	6500	5500	22.2	55.5	117.11	164.24	118.25	9, 16
Long Haul Tractor Trailer	14400	25600	36.2	90.5	190.96	267.81	192.83	9, 16
Small Tanker	1.1×10^7	4.6×10^7	3124	7810	16479.10	23111.94	16640.60	10, 16
Ferry	8.0×10^6	5.853×10^5	5151	12877.5	27171.53	38108.06	27437.81	11, 16
Cruise ship	1.0×10^8	7.92×10^5	23463	58657.5	123767.33	173583.67	124980.24	12, 16
Train	4.5×10^5	5.77×10^5	282.73	707	1491.40	2091.69	1506.02	13-16

Table F: Percent added weight of CO₂ capture system and liquid storage (CCS-LS) with respect to total weight and payload of different vehicles (M_{AD} , V_{AD} : mass and volume of adsorbent)

	Travel	Diesel	Product	M_{AD}, kg	V_{AD}, l	CCS-LS	CCS-LS	CCS-LS	CCS-LS
	Time	Used	CO₂ per			Weight, kg	Volume, l	Weight /	Weight /
		per	hour, kg					Payload	Total
		hour, l							Weight
Car	4	4.06	8.57	85.72	106.48	154.63	154.57	34.06	7.25
SUV	4	6.88	14.51	145.06	180.20	261.68	261.58	38.48	10.79
Pickup Truck	4	8.13	17.14	171.44	212.97	309.26	309.14	18.43	7.29
Van/Minibus	8	3.44	7.25	72.53	90.10	189.15	171.48	7.94	3.11
School Bus	8	6.88	14.51	145.06	180.20	378.30	342.96	7.25	3.40
City Bus	8	18.13	38.24	382.44	475.08	997.34	904.17	11.89	6.98
City Hybrid Bus	8	14.06	29.67	296.72	368.59	773.80	701.51	9.22	5.42
City Delivery	8	6.63	13.98	139.79	173.65	364.54	330.49	9.24	4.36
Regional Delivery Truck	4	13.88	29.28	292.76	363.68	528.12	527.92	9.60	4.40
Long Haul Tractor Trailer	4	22.63	47.74	477.39	593.03	861.17	860.84	3.36	2.15
Small Tanker	14	557.86	1177.08	11770.79	14622.09	44890.48	37734.03	0.10	0.08
Ferry	8	1609.69	3396.44	33964.41	42191.81	88573.74	80299.87	15.13	1.03
Cruise ship	8	7332.19	15470.92	154709.16	192185.29	403456.73	365768.96	50.94	0.40
Train	4	176.71	372.85	3728.50	4631.68	6725.92	6723.37	1.17	0.65

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