

## Supplementary Material

### 1 Supplementary Data

#### Mass isotopomer-balance equations for C8:0 :

$$\begin{aligned}
 \frac{d}{dt} [C8:0_0] &= \frac{1}{C8:0} \left( F_5 \left[ \begin{smallmatrix} C8:0_0^{medium} \\ C8:0_8^{medium} \end{smallmatrix} \right] - F_5^{inv} \left[ \begin{smallmatrix} C8:0_0 \\ C8:0_8 \end{smallmatrix} \right] - F_6 \left[ \begin{smallmatrix} C8:0_0 \\ C8:0_8 \end{smallmatrix} \right] + F_6^{inv} \left[ \begin{smallmatrix} 3OHC8:0_0 \\ 3OHC8:0_8 \end{smallmatrix} \right] \right) \\
 \frac{d}{dt} [3OHC8:0_0] &= \frac{1}{3OHC8:0} \left( F_6 \left[ \begin{smallmatrix} C8:0_0 \\ C8:0_8 \end{smallmatrix} \right] - F_6^{inv} \left[ \begin{smallmatrix} 3OHC8:0_0 \\ 3OHC8:0_8 \end{smallmatrix} \right] - F_8 \left[ \begin{smallmatrix} 3OHC8:0_0 \\ 3OHC8:0_8 \end{smallmatrix} \right] + F_8^{inv} \left[ \begin{smallmatrix} C6:0_0 \cdot AcCoA_0 \\ C6:0_6 \cdot AcCoA_2 \end{smallmatrix} \right] - F_7 \left[ \begin{smallmatrix} 3OHC8:0_0 \\ 3OHC8:0_8 \end{smallmatrix} \right] \right) \\
 \frac{d}{dt} [C6:0_0] &= \frac{1}{C6:0} \left( F_8 \left[ \begin{smallmatrix} 3OHC8:0_0 \\ 3OHC8:0_8 \end{smallmatrix} \right] - F_8^{inv} \left[ \begin{smallmatrix} C6:0_0 \\ C6:0_6 \end{smallmatrix} \right] - F_{10} \left[ \begin{smallmatrix} C6:0_0 \\ C6:0_6 \end{smallmatrix} \right] + F_{10}^{inv} \left[ \begin{smallmatrix} 3OHC6:0_0 \\ 3OHC6:0_6 \end{smallmatrix} \right] - F_9 \left[ \begin{smallmatrix} C6:0_0 \\ C6:0_6 \end{smallmatrix} \right] \right) \\
 \frac{d}{dt} [3OHC6:0_0] &= \frac{1}{3OHC6:0} \left( F_{10} \left[ \begin{smallmatrix} C6:0_0 \\ C6:0_6 \end{smallmatrix} \right] - F_{10}^{inv} \left[ \begin{smallmatrix} 3OHC6:0_0 \\ 3OHC6:0_6 \end{smallmatrix} \right] - F_{12} \left[ \begin{smallmatrix} 3OHC6:0_0 \\ 3OHC6:0_6 \end{smallmatrix} \right] + F_{12}^{inv} \left[ \begin{smallmatrix} AcCoA_0 \cdot AcCoA_0 \cdot AcCoA_0 \\ AcCoA_2 \cdot AcCoA_2 \cdot AcCoA_2 \end{smallmatrix} \right] - F_{11} \left[ \begin{smallmatrix} 3OHC6:0_0 \\ 3OHC6:0_6 \end{smallmatrix} \right] \right) \\
 \frac{d}{dt} [AcCoA_0] &= \frac{1}{AcCoA} \left( F_8 \left[ \begin{smallmatrix} 3OHC8:0_0 \\ 3OHC8:0_8 \end{smallmatrix} \right] - F_8^{inv} \left[ \begin{smallmatrix} AcCoA_0 \\ AcCoA_2 \end{smallmatrix} \right] + F_{12} \left[ \begin{smallmatrix} 3OHC6:0_0 \\ 3OHC6:0_6 \end{smallmatrix} \right] - F_{12}^{inv} \left[ \begin{smallmatrix} AcCoA_0 \cdot AcCoA_0 \cdot AcCoA_0 \\ AcCoA_2 \cdot AcCoA_2 \cdot AcCoA_2 \end{smallmatrix} \right] - F_{14} \left[ \begin{smallmatrix} AcCoA_0 \cdot AcCoA_0 \\ AcCoA_2 \cdot AcCoA_2 \end{smallmatrix} \right] + F_{13} \left[ \begin{smallmatrix} 1 \\ 0 \end{smallmatrix} \right] \right)
 \end{aligned}$$

#### Mass isotopomer-balance equations for C10:0:

$$\begin{aligned}
 \frac{d}{dt} [C10:0_0] &= \frac{1}{C10:0} \left( F_1 \left[ \begin{smallmatrix} C10:0_0^{medium} \\ C10:0_{10}^{medium} \end{smallmatrix} \right] - F_1^{inv} \left[ \begin{smallmatrix} C10:0_0 \\ C10:0_{10} \end{smallmatrix} \right] - F_2 \left[ \begin{smallmatrix} C10:0_0 \\ C10:0_{10} \end{smallmatrix} \right] + F_2^{inv} \left[ \begin{smallmatrix} 3OHC10:0_0 \\ 3OHC10:0_{10} \end{smallmatrix} \right] \right) \\
 \frac{d}{dt} [3OHC10:0_0] &= \frac{1}{3OHC10:0} \left( F_2 \left[ \begin{smallmatrix} C10:0_0 \\ C10:0_{10} \end{smallmatrix} \right] - F_2^{inv} \left[ \begin{smallmatrix} 3OHC10:0_0 \\ 3OHC10:0_{10} \end{smallmatrix} \right] - F_4 \left[ \begin{smallmatrix} 3OHC10:0_0 \\ 3OHC10:0_{10} \end{smallmatrix} \right] + F_4^{inv} \left[ \begin{smallmatrix} C8:0_0 \cdot AcCoA_0 \\ C8:0_8 \cdot AcCoA_2 \end{smallmatrix} \right] - F_3 \left[ \begin{smallmatrix} 3OHC10:0_0 \\ 3OHC10:0_{10} \end{smallmatrix} \right] \right) \\
 \frac{d}{dt} [C8:0_0] &= \frac{1}{C8:0} \left( F_4 \left[ \begin{smallmatrix} 3OHC10:0_0 \\ 3OHC10:0_{10} \end{smallmatrix} \right] - F_4^{inv} \left[ \begin{smallmatrix} C8:0_0 \\ C8:0_8 \end{smallmatrix} \right] - F_6 \left[ \begin{smallmatrix} C8:0_0 \\ C8:0_8 \end{smallmatrix} \right] + F_6^{inv} \left[ \begin{smallmatrix} 3OHC8:0_0 \\ 3OHC8:0_8 \end{smallmatrix} \right] - F_5^{inv} \left[ \begin{smallmatrix} C8:0_0 \\ C8:0_8 \end{smallmatrix} \right] \right) \\
 \frac{d}{dt} [3OHC8:0_0] &= \frac{1}{3OHC8:0} \left( F_6 \left[ \begin{smallmatrix} C8:0_0 \\ C8:0_8 \end{smallmatrix} \right] - F_6^{inv} \left[ \begin{smallmatrix} 3OHC8:0_0 \\ 3OHC8:0_8 \end{smallmatrix} \right] - F_8 \left[ \begin{smallmatrix} 3OHC8:0_0 \\ 3OHC8:0_8 \end{smallmatrix} \right] + F_8^{inv} \left[ \begin{smallmatrix} C6:0_0 \cdot AcCoA_0 \\ C6:0_6 \cdot AcCoA_2 \end{smallmatrix} \right] - F_7 \left[ \begin{smallmatrix} 3OHC8:0_0 \\ 3OHC8:0_8 \end{smallmatrix} \right] \right) \\
 \frac{d}{dt} [C6:0_0] &= \frac{1}{C6:0} \left( F_8 \left[ \begin{smallmatrix} 3OHC8:0_0 \\ 3OHC8:0_8 \end{smallmatrix} \right] - F_8^{inv} \left[ \begin{smallmatrix} C6:0_0 \\ C6:0_6 \end{smallmatrix} \right] - F_{10} \left[ \begin{smallmatrix} C6:0_0 \\ C6:0_6 \end{smallmatrix} \right] + F_{10}^{inv} \left[ \begin{smallmatrix} 3OHC6:0_0 \\ 3OHC6:0_6 \end{smallmatrix} \right] - F_9 \left[ \begin{smallmatrix} C6:0_0 \\ C6:0_6 \end{smallmatrix} \right] \right) \\
 \frac{d}{dt} [3OHC6:0_0] &= \frac{1}{3OHC6:0} \left( F_{10} \left[ \begin{smallmatrix} C6:0_0 \\ C6:0_6 \end{smallmatrix} \right] - F_{10}^{inv} \left[ \begin{smallmatrix} 3OHC6:0_0 \\ 3OHC6:0_6 \end{smallmatrix} \right] - F_{12} \left[ \begin{smallmatrix} 3OHC6:0_0 \\ 3OHC6:0_6 \end{smallmatrix} \right] + F_{12}^{inv} \left[ \begin{smallmatrix} AcCoA_0 \cdot AcCoA_0 \cdot AcCoA_0 \\ AcCoA_2 \cdot AcCoA_2 \cdot AcCoA_2 \end{smallmatrix} \right] - F_{11} \left[ \begin{smallmatrix} 3OHC6:0_0 \\ 3OHC6:0_6 \end{smallmatrix} \right] \right)
 \end{aligned}$$

$$\frac{d}{dt} \left[ \frac{AcCoA_0}{AcCoA_2} \right] = \frac{1}{AcCoA} \left( F_4 \begin{bmatrix} 3OHC10:0_0 \\ 3OHC10:0_{10} \end{bmatrix} - F_4^{inv} \begin{bmatrix} AcCoA_0 \\ AcCoA_2 \end{bmatrix} + F_8 \begin{bmatrix} 3OHC8:0_0 \\ 3OHC8:0_8 \end{bmatrix} - F_8^{inv} \begin{bmatrix} AcCoA_0 \\ AcCoA_2 \end{bmatrix} + F_{12} \begin{bmatrix} 3OHC6:0_0 \\ 3OHC6:0_6 \end{bmatrix} \right. \\ \left. - F_{12}^{inv} \begin{bmatrix} AcCoA_0 \cdot AcCoA_0 \cdot AcCoA_0 \\ AcCoA_2 \cdot AcCoA_2 \cdot AcCoA_2 \end{bmatrix} - F_{14} \begin{bmatrix} AcCoA_0 \cdot AcCoA_0 \\ AcCoA_2 \cdot AcCoA_2 \end{bmatrix} + F_{13} \begin{bmatrix} 1 \\ 0 \end{bmatrix} \right)$$

## 2 Supplementary Table

|                                                  | C8:0   |       | C10:0  |          |
|--------------------------------------------------|--------|-------|--------|----------|
|                                                  | flux   | SD    | flux   | SD       |
| F <sub>1</sub>                                   | NA     | NA    | 0.217  | 0.069    |
| F <sub>1</sub> <sup>inv</sup>                    | NA     | NA    | 0.236  | 0.077    |
| F <sub>2</sub>                                   | NA     | NA    | 0.012  | 0.004    |
| F <sub>2</sub> <sup>inv</sup>                    | NA     | NA    | 0.027  | 0.010    |
| F <sub>4</sub>                                   | NA     | NA    | 0.020  | 0.014    |
| F <sub>4</sub> <sup>inv</sup>                    | NA     | NA    | 0.045  | 0.015    |
| F <sub>5</sub>                                   | 0.135  | 0.029 | NA     | NA       |
| F <sub>5</sub> <sup>inv</sup>                    | 0.080  | 0.031 | NA     | NA       |
| F <sub>6</sub>                                   | 0.098  | 0.014 | 0.091  | 0.131    |
| F <sub>6</sub> <sup>inv</sup>                    | 0.043  | 0.011 | 0.238  | 0.129**  |
| F <sub>8</sub>                                   | 0.140  | 0.030 | 0.000  | 0.000*** |
| F <sub>8</sub> <sup>inv</sup>                    | 0.109  | 0.027 | 0.221  | 0.074**  |
| F <sub>10</sub>                                  | 0.532  | 0.379 | 0.000  | 0.000**  |
| F <sub>10</sub> <sup>inv</sup>                   | 0.877  | 0.452 | 0.241  | 0.057**  |
| F <sub>12</sub>                                  | 0.000  | 0.000 | 0.708  | 0.666*   |
| F <sub>12</sub> <sup>inv</sup>                   | 0.147  | 0.031 | 0.930  | 0.644**  |
| F <sub>13</sub>                                  | 0.187  | 0.017 | 0.490  | 0.045*** |
| Calculated differences                           |        |       |        |          |
| F <sub>6</sub> - F <sub>6</sub> <sup>inv</sup>   | 0.056  | 0.018 | -0.147 | 0.184**  |
| F <sub>8</sub> - F <sub>8</sub> <sup>inv</sup>   | 0.031  | 0.041 | -0.221 | 0.074*   |
| F <sub>10</sub> - F <sub>10</sub> <sup>inv</sup> | -0.345 | 0.590 | -0.241 | 0.057    |
| F <sub>12</sub> - F <sub>12</sub> <sup>inv</sup> | -0.147 | 0.031 | -0.222 | 0.926    |

Table S1 : Fluxes (in  $\mu\text{mol/g prot/min}$ ) resulting from the best fit of the mathematical model of  $\beta$ -oxidation. NA : non-available. \*  $p < 0.05$ ; \*\*  $p < 0.01$ ; \*\*\* $p < 0.001$

### 3 Supplementary Figure

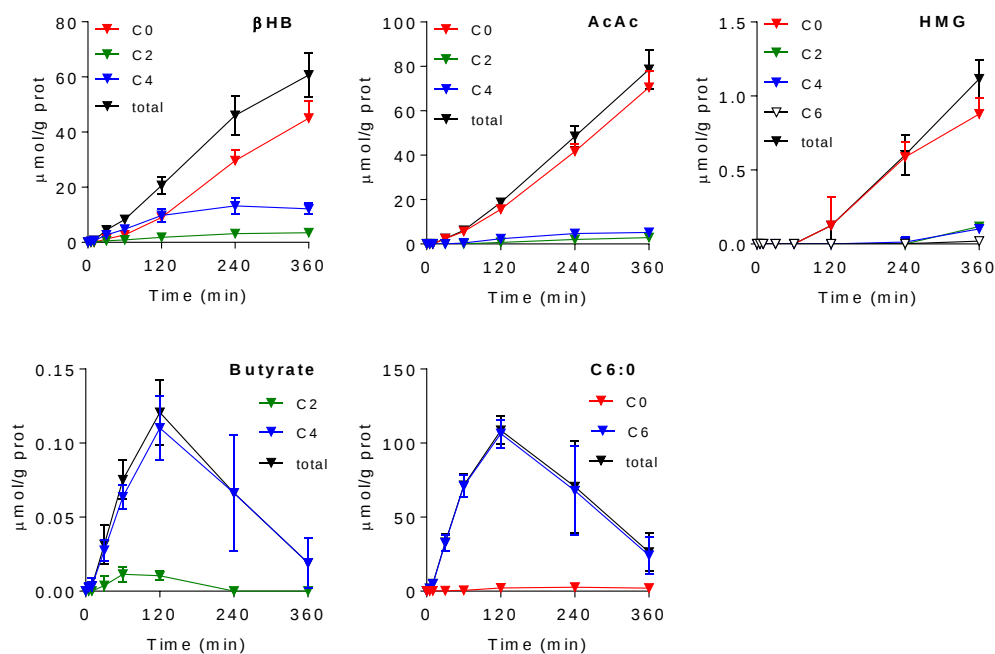


Figure S1 : Secretion rates of selected ketone bodies, HMG, butyrate and C6:0 determined from the total extracellular concentrations experimentally measured in HepG2 cells incubated with [U- $^{13}\text{C}$ ]-C8:0 (mean $\pm$ SD, n=3). Secretion of  $\beta\text{HB}$  and AcAc was detected at time 5 min and 30 min, respectively, consistent with the general observation that the liver is the major organ for ketone production (Evans et al., 2017). Secretion of HMG, butyrate and C6:0 was detected at 120 min, 5 min and 5 min, respectively. Detection of mass isotopomers for HMG and butyrate was different as compared to iPSC astrocytes. Concentrations of butyrate and C6:0 peaked at 120 min and then decreased (inverted U-shape). All together, these data show different metabolite quantification in different cell types under similar conditions, supporting the sensitivity and the specificity of the measurements.